

# Mathematica 11.3 Integration Test Results

Test results for the 4 problems in "4.2.2.2 (g sin)<sup>p</sup> (a+b cos)<sup>m</sup> (c+d cos)<sup>n</sup>.m"

Problem 1: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sqrt{d \cos[e+f x]} \sqrt{g \sin[e+f x]}}{a + b \cos[e+f x]} dx$$

Optimal (type 4, 509 leaves, 16 steps):

$$\begin{aligned} & -\frac{\sqrt{d} \sqrt{g} \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{d} \sqrt{g \sin[e+f x]}}{\sqrt{g} \sqrt{d \cos[e+f x]}}\right]}{\sqrt{2} b f}+\frac{\sqrt{d} \sqrt{g} \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{d} \sqrt{g \sin[e+f x]}}{\sqrt{g} \sqrt{d \cos[e+f x]}}\right]}{\sqrt{2} b f}+ \\ & \frac{2 \sqrt{2} a d \sqrt{g} \sqrt{\cos[e+f x]} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \sin[e+f x]}}{\sqrt{g} \sqrt{1+\cos[e+f x]}}\right], -1\right]}{b \sqrt{-a+b} \sqrt{a+b} f \sqrt{d \cos[e+f x]}}- \\ & \frac{2 \sqrt{2} a d \sqrt{g} \sqrt{\cos[e+f x]} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \sin[e+f x]}}{\sqrt{g} \sqrt{1+\cos[e+f x]}}\right], -1\right]}{b \sqrt{-a+b} \sqrt{a+b} f \sqrt{d \cos[e+f x]}}+ \\ & \frac{\sqrt{d} \sqrt{g} \operatorname{Log}\left[\sqrt{g}-\frac{\sqrt{2} \sqrt{d} \sqrt{g \sin[e+f x]}}{\sqrt{d \cos[e+f x]}}+\sqrt{g} \tan[e+f x]\right]}{2 \sqrt{2} b f}- \\ & \frac{\sqrt{d} \sqrt{g} \operatorname{Log}\left[\sqrt{g}+\frac{\sqrt{2} \sqrt{d} \sqrt{g \sin[e+f x]}}{\sqrt{d \cos[e+f x]}}+\sqrt{g} \tan[e+f x]\right]}{2 \sqrt{2} b f} \end{aligned}$$

Result (type 4, 272 leaves):

$$\begin{aligned}
& \frac{1}{\sqrt{-a-b} \sqrt{a-b} b f \sqrt{\frac{\cos[e+f x]}{1+\cos[e+f x]}} \sqrt{g \sin[e+f x]}} \\
& 2 \sqrt{2} g \sqrt{d \cos[e+f x]} \left( -\text{i} \sqrt{-a-b} \sqrt{a-b} \text{EllipticPi}\left[-\text{i}, -\text{ArcSin}\left[\sqrt{\tan\left[\frac{1}{2}(e+f x)\right]}, -1\right]\right. \right. \\
& \left. \left. + \text{i} \sqrt{-a-b} \sqrt{a-b} \text{EllipticPi}\left[\text{i}, -\text{ArcSin}\left[\sqrt{\tan\left[\frac{1}{2}(e+f x)\right]}, -1\right]\right] + \right. \right. \\
& a \left( \text{EllipticPi}\left[-\frac{\sqrt{a-b}}{\sqrt{-a-b}}, -\text{ArcSin}\left[\sqrt{\tan\left[\frac{1}{2}(e+f x)\right]}, -1\right]\right. \right. \\
& \left. \left. - \text{EllipticPi}\left[\frac{\sqrt{a-b}}{\sqrt{-a-b}}, -\text{ArcSin}\left[\sqrt{\tan\left[\frac{1}{2}(e+f x)\right]}, -1\right]\right]\right) \sqrt{\tan\left[\frac{1}{2}(e+f x)\right]}
\end{aligned}$$

**Problem 2:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{d \cos[e+f x]}}{(a+b \cos[e+f x]) \sqrt{g \sin[e+f x]}} dx$$

Optimal (type 4, 209 leaves, 4 steps):

$$\begin{aligned}
& \frac{2 \sqrt{2} \sqrt{d} \text{EllipticPi}\left[-\frac{a}{b-\sqrt{-a^2+b^2}}, \text{ArcSin}\left[\frac{\sqrt{d \cos[e+f x]}}{\sqrt{d} \sqrt{1+\sin[e+f x]}}, -1\right]\right] \sqrt{\sin[e+f x]}}{\sqrt{-a^2+b^2} f \sqrt{g \sin[e+f x]}} \\
& \frac{2 \sqrt{2} \sqrt{d} \text{EllipticPi}\left[-\frac{a}{b+\sqrt{-a^2+b^2}}, \text{ArcSin}\left[\frac{\sqrt{d \cos[e+f x]}}{\sqrt{d} \sqrt{1+\sin[e+f x]}}, -1\right]\right] \sqrt{\sin[e+f x]}}{\sqrt{-a^2+b^2} f \sqrt{g \sin[e+f x]}}
\end{aligned}$$

Result (type 6, 594 leaves):

$$\begin{aligned}
& \frac{1}{f(a + b \cos[e + f x]) \sqrt{g \sin[e + f x]} (1 + \tan[e + f x]^2)^{3/2}} \\
& 2 \sqrt{d \cos[e + f x]} \sec[e + f x]^2 \sqrt{\tan[e + f x]} \left( b + a \sqrt{1 + \tan[e + f x]^2} \right) \left( \frac{1}{4 \sqrt{2} (a^2 - b^2)^{3/4}} \right. \\
& \sqrt{a} \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\tan[e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\tan[e + f x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \\
& \left. \log \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} + a \tan[e + f x] \right] + \right. \\
& \left. \log \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} + a \tan[e + f x] \right] \right) + \\
& \left( 5 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, -\tan[e + f x]^2, -\frac{a^2 \tan[e + f x]^2}{a^2 - b^2} \right] \sqrt{\tan[e + f x]} \right) / \\
& \left( \sqrt{1 + \tan[e + f x]^2} \left( -5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, -\tan[e + f x]^2, -\frac{a^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
& 2 \left( 2 a^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, -\tan[e + f x]^2, -\frac{a^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \\
& \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, -\frac{a^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \\
& \left. \tan[e + f x]^2 \right) (-b^2 + a^2 (1 + \tan[e + f x]^2)) \right)
\end{aligned}$$

**Problem 3: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{g \sin[e + f x]}}{\sqrt{d \cos[e + f x]} (a + b \cos[e + f x])} dx$$

Optimal (type 4, 208 leaves, 5 steps):

$$\begin{aligned}
& - \left( \left( 2 \sqrt{2} \sqrt{g} \sqrt{\cos[e + f x]} \operatorname{EllipticPi} \left[ -\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin} \left[ \frac{\sqrt{g \sin[e + f x]}}{\sqrt{g} \sqrt{1 + \cos[e + f x]}} \right], -1 \right] \right) / \right. \\
& \left. \left( \sqrt{-a+b} \sqrt{a+b} f \sqrt{d \cos[e + f x]} \right) + \right. \\
& \left. \left( 2 \sqrt{2} \sqrt{g} \sqrt{\cos[e + f x]} \operatorname{EllipticPi} \left[ \frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin} \left[ \frac{\sqrt{g \sin[e + f x]}}{\sqrt{g} \sqrt{1 + \cos[e + f x]}} \right], -1 \right] \right) / \right. \\
& \left. \left( \sqrt{-a+b} \sqrt{a+b} f \sqrt{d \cos[e + f x]} \right) \right)
\end{aligned}$$

Result (type 6, 596 leaves):

**Problem 4:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{d \cos[e + f x] - (a + b \cos[e + f x])} \sqrt{g \sin[e + f x]}} dx$$

Optimal (type 4, 273 leaves, 7 steps):

$$\begin{aligned}
& - \left( \left( 2 \sqrt{2} b \operatorname{EllipticPi} \left[ -\frac{a}{b - \sqrt{-a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{d} \cos[e + fx]}{\sqrt{d} \sqrt{1 + \sin[e + fx]}} \right], -1 \right] \sqrt{\sin[e + fx]} \right) \right. \\
& \quad \left. \left( a \sqrt{-a^2 + b^2} \sqrt{d} f \sqrt{g \sin[e + fx]} \right) \right) + \\
& \left( 2 \sqrt{2} b \operatorname{EllipticPi} \left[ -\frac{a}{b + \sqrt{-a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{d} \cos[e + fx]}{\sqrt{d} \sqrt{1 + \sin[e + fx]}} \right], -1 \right] \sqrt{\sin[e + fx]} \right) / \\
& \quad \left( a \sqrt{-a^2 + b^2} \sqrt{d} f \sqrt{g \sin[e + fx]} \right) + \frac{\operatorname{EllipticF} \left[ e - \frac{\pi}{4} + fx, 2 \right] \sqrt{\sin[2e + 2fx]}}{a f \sqrt{d \cos[e + fx]} \sqrt{g \sin[e + fx]}}
\end{aligned}$$

### Result (type 6, 5869 leaves) :

$$\begin{aligned}
& \left( 4 (a+b) \cos \left[ \frac{1}{2} (e+f x) \right]^3 \sin \left[ \frac{1}{2} (e+f x) \right] \right. \\
& \left. \left( 25 \text{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, -\frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \right) / \right. \\
& \left. \left( 5 (a+b) \text{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, -\frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + \right. \right. \\
& \left. \left. 2 \left( -2 (a-b) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, -\frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + \right. \right. \\
& \left. \left. (a+b) \text{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, -\frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \right) + \right. \\
& \left. \left. \tan \left[ \frac{1}{2} (e+f x) \right]^2 \right) + \left( 9 \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (e+f x) \right]^2 \right) / \right. \\
& \left. \left( 9 (a+b) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, -\frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + \right. \right. \\
& \left. \left. 2 \left( -2 (a-b) \text{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, -\frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + \right. \right. \\
& \left. \left. (a+b) \text{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \\
& \left. \left. -\frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (e+f x) \right]^2 \right) \right) \right) / \right. \\
& \left. \left( 5 f \sqrt{\cos [e+f x]} \sqrt{d \cos [e+f x]} (a+b \cos [e+f x])^2 \sqrt{\sin [e+f x]} \right. \right. \\
& \left. \left. \sqrt{g \sin [e+f x]} \right. \right. \\
& \left. \left. -\frac{1}{5 (a+b \cos [e+f x]) \sin [e+f x]^{3/2}} \right. \right. \\
& \left. \left. 2 (a+b) \cos \left[ \frac{1}{2} (e+f x) \right]^3 \sqrt{\cos [e+f x]} \sin \left[ \frac{1}{2} (e+f x) \right] \right. \right. \\
& \left. \left. \left( 25 \text{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, -\frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \right) \right) / \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 5 (a+b) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + \right. \\
& \quad 2 \left( -2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \\
& \quad \left. \left. - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (e+f x) \right]^2 \Bigg) + \\
& \left( 9 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (e+f x) \right]^2 \right) / \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \\
& \quad \left. \left. - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + 2 \left( -2 (a-b) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \right. \right. \\
& \quad \left. \left. \frac{13}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (e+f x) \right]^2 \right) + \\
& \frac{1}{5 \sqrt{\cos [e+f x]} (a+b \cos [e+f x]) \sqrt{\sin [e+f x]}} 2 (a+b) \cos \left[ \frac{1}{2} (e+f x) \right]^4 \\
& \left( \left( 25 \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \right) / \right. \\
& \quad \left( 5 (a+b) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + \right. \\
& \quad 2 \left( -2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + \right. \\
& \quad \left. (a+b) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \right) \\
& \quad \tan \left[ \frac{1}{2} (e+f x) \right]^2 \Bigg) + \left( 9 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
& - \frac{(\mathbf{a} - \mathbf{b}) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2}{\mathbf{a} + \mathbf{b}} \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2 \Bigg) \Bigg/ \\
& \left( 9 (\mathbf{a} + \mathbf{b}) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2, - \frac{(\mathbf{a} - \mathbf{b}) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2}{\mathbf{a} + \mathbf{b}}\right] + \right. \\
& 2 \left( -2 (\mathbf{a} - \mathbf{b}) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2, \right. \right. \\
& \left. \left. - \frac{(\mathbf{a} - \mathbf{b}) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2}{\mathbf{a} + \mathbf{b}}\right] + (\mathbf{a} + \mathbf{b}) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2, - \frac{(\mathbf{a} - \mathbf{b}) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2}{\mathbf{a} + \mathbf{b}}\right] \right) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2 \Bigg) \Bigg) - \\
& \frac{1}{5 \sqrt{\operatorname{Cos}[\mathbf{e} + \mathbf{f} x]} (\mathbf{a} + \mathbf{b} \operatorname{Cos}[\mathbf{e} + \mathbf{f} x]) \sqrt{\operatorname{Sin}[\mathbf{e} + \mathbf{f} x]}} 6 (\mathbf{a} + \mathbf{b}) \operatorname{Cos}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2 \\
& \operatorname{Sin}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2 \\
& \left( \left( 25 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2, - \frac{(\mathbf{a} - \mathbf{b}) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2}{\mathbf{a} + \mathbf{b}}\right] \right) \Bigg/ \right. \\
& \left. \left( 5 (\mathbf{a} + \mathbf{b}) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2, - \frac{(\mathbf{a} - \mathbf{b}) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2}{\mathbf{a} + \mathbf{b}}\right] + \right. \right. \\
& 2 \left( -2 (\mathbf{a} - \mathbf{b}) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2, - \frac{(\mathbf{a} - \mathbf{b}) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2}{\mathbf{a} + \mathbf{b}}\right] + \right. \\
& (\mathbf{a} + \mathbf{b}) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2, - \frac{(\mathbf{a} - \mathbf{b}) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2}{\mathbf{a} + \mathbf{b}}\right] \Bigg) \\
& \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2 \Bigg) + \left( 9 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2, \right. \right. \\
& \left. \left. - \frac{(\mathbf{a} - \mathbf{b}) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2}{\mathbf{a} + \mathbf{b}}\right] \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2 \Bigg) \Bigg/ \\
& \left( 9 (\mathbf{a} + \mathbf{b}) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2, - \frac{(\mathbf{a} - \mathbf{b}) \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2}{\mathbf{a} + \mathbf{b}}\right] + \right. \\
& 2 \left( -2 (\mathbf{a} - \mathbf{b}) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{2} (\mathbf{e} + \mathbf{f} x)\right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
& - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2}{a+b} ] + (a+b) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \right. \\
& \left. \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2 \Bigg) + \\
& \frac{1}{5 \sqrt{\cos[e+f x]} (a+b \cos[e+f x])^2} 4 b (a+b) \cos\left[\frac{1}{2} (e+f x)\right]^3 \\
& \sin\left[\frac{1}{2} (e+f x)\right] \sqrt{\sin[e+f x]} \\
& \left( \left( 25 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2}{a+b} \right] \right) / \right. \\
& \left. \left( 5 (a+b) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2}{a+b} \right] + \right. \right. \\
& 2 \left( -2 (a-b) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2}{a+b} \right] + \right. \\
& (a+b) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2}{a+b} \right] \Bigg) \\
& \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2 \Bigg) + \left( 9 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, \right. \right. \\
& \left. \left. - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2 \right) / \\
& \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2}{a+b} \right] + \right. \\
& 2 \left( -2 (a-b) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, \right. \right. \\
& \left. \left. - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2 \right) \Bigg) + \\
& \frac{1}{5 \cos[e+f x]^{3/2} (a+b \cos[e+f x])} 2 (a+b) \cos\left[\frac{1}{2} (e+f x)\right]^3 \sin\left[\frac{1}{2} (e+f x)\right] \\
& \sqrt{\sin[e+f x]}
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 25 \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, -\frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] \right) / \right. \\
& \left. \left( 5 (\mathbf{a} + \mathbf{b}) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, -\frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] + \right. \right. \\
& \left. \left. 2 \left( -2 (\mathbf{a} - \mathbf{b}) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, -\frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] + \right. \right. \\
& \left. \left. (\mathbf{a} + \mathbf{b}) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, -\frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] \right) + \right. \\
& \left. \left. \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2 \right) + \left( 9 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, \right. \right. \\
& \left. \left. -\frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2 \right) / \right. \\
& \left. \left( 9 (\mathbf{a} + \mathbf{b}) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, -\frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] + \right. \right. \\
& \left. \left. 2 \left( -2 (\mathbf{a} - \mathbf{b}) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] + (\mathbf{a} + \mathbf{b}) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \right. \right. \\
& \left. \left. \left. \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, -\frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] \right) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2 \right) \right) + \\
& \frac{1}{5 \sqrt{\cos[\mathbf{e} + \mathbf{f} x]} (\mathbf{a} + \mathbf{b} \cos[\mathbf{e} + \mathbf{f} x]) \sqrt{\sin[\mathbf{e} + \mathbf{f} x]}} 4 (\mathbf{a} + \mathbf{b}) \cos \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^3 \\
& \sin \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right] \\
& \left( \left( 25 \left( -\frac{1}{5 (\mathbf{a} + \mathbf{b})} (\mathbf{a} - \mathbf{b}) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. -\frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] \sec \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2 \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right] + \right. \right. \\
& \left. \left. \left. \left. \frac{1}{10} \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, -\frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{\sec[\frac{1}{2}(e+f x)]^2 \tan[\frac{1}{2}(e+f x)]}{\left(5(a+b) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan[\frac{1}{2}(e+f x)]^2, -\frac{(a-b) \tan[\frac{1}{2}(e+f x)]^2}{a+b}\right] + \right. \right. \right. \\
& \left. \left. \left. 2 \left( -2(a-b) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \tan[\frac{1}{2}(e+f x)]^2, -\frac{(a-b) \tan[\frac{1}{2}(e+f x)]^2}{a+b}\right] + \right. \right. \right. \\
& \left. \left. \left. (a+b) \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \tan[\frac{1}{2}(e+f x)]^2, -\frac{(a-b) \tan[\frac{1}{2}(e+f x)]^2}{a+b}\right]\right) \right. \right. \\
& \left. \left. \left. \tan[\frac{1}{2}(e+f x)]^2 \right) + \left( 9 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan[\frac{1}{2}(e+f x)]^2, \right. \right. \right. \\
& \left. \left. \left. -\frac{(a-b) \tan[\frac{1}{2}(e+f x)]^2}{a+b}\right] \sec[\frac{1}{2}(e+f x)]^2 \tan[\frac{1}{2}(e+f x)] \right) \right. \right. \\
& \left. \left. \left. \left( 9(a+b) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan[\frac{1}{2}(e+f x)]^2, -\frac{(a-b) \tan[\frac{1}{2}(e+f x)]^2}{a+b}\right] + \right. \right. \right. \\
& \left. \left. \left. 2 \left( -2(a-b) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \tan[\frac{1}{2}(e+f x)]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. -\frac{(a-b) \tan[\frac{1}{2}(e+f x)]^2}{a+b}\right] + (a+b) \text{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \right. \right. \right. \\
& \left. \left. \left. \tan[\frac{1}{2}(e+f x)]^2, -\frac{(a-b) \tan[\frac{1}{2}(e+f x)]^2}{a+b}\right] \right) \tan[\frac{1}{2}(e+f x)]^2 \right) + \right. \right. \\
& \left. \left. \left. \left( 9 \tan[\frac{1}{2}(e+f x)]^2 \left( -\frac{1}{9(a+b)} 5(a-b) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \tan[\frac{1}{2}(e+f x)]^2, -\frac{(a-b) \tan[\frac{1}{2}(e+f x)]^2}{a+b}\right] \sec[\frac{1}{2}(e+f x)]^2 \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \tan[\frac{1}{2}(e+f x)]^2 + \frac{5}{18} \text{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \tan[\frac{1}{2}(e+f x)]^2, \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. -\frac{(a-b) \tan[\frac{1}{2}(e+f x)]^2}{a+b}\right] \sec[\frac{1}{2}(e+f x)]^2 \tan[\frac{1}{2}(e+f x)] \right) \right) \right) \right. \right. \\
& \left. \left. \left. \left. \left. \left( 9(a+b) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan[\frac{1}{2}(e+f x)]^2, -\frac{(a-b) \tan[\frac{1}{2}(e+f x)]^2}{a+b}\right] + \right. \right. \right. \right. \right. \\
\end{aligned}$$

$$\begin{aligned}
& 2 \left( -2 (a-b) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \\
& \quad \left. \left. - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (e+f x) \right]^2 \right) - \\
& \left( 25 \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \left( 2 \left( -2 (a-b) \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] + \right. \\
& \quad \left. \left. (a+b) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \right) \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (e+f x) \right]^2 \tan \left[ \frac{1}{2} (e+f x) \right] + 5 (a+b) \left( - \frac{1}{5 (a+b)} (a-b) \operatorname{AppellF1} \left[ \frac{5}{4}, \right. \right. \right. \\
& \quad \left. \left. \frac{1}{2}, 2, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (e+f x) \right]^2 \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (e+f x) \right] + \frac{1}{10} \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \\
& \quad \left. \left. - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (e+f x) \right]^2 \tan \left[ \frac{1}{2} (e+f x) \right] \right) + \\
& 2 \tan \left[ \frac{1}{2} (e+f x) \right]^2 \left( -2 (a-b) \left( - \frac{1}{9 (a+b)} 10 (a-b) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 3, \right. \right. \right. \\
& \quad \left. \left. \frac{13}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (e+f x) \right]^2 \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (e+f x) \right] + \frac{5}{18} \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 2, \frac{13}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \\
& \quad \left. \left. - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (e+f x) \right]^2 \tan \left[ \frac{1}{2} (e+f x) \right] \right) + \\
& (a+b) \left( - \frac{1}{9 (a+b)} 5 (a-b) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 2, \frac{13}{4}, \tan \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \\
& \quad \left. \left. - \frac{(a-b) \tan \left[ \frac{1}{2} (e+f x) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (e+f x) \right]^2 \tan \left[ \frac{1}{2} (e+f x) \right] + \right)
\end{aligned}$$

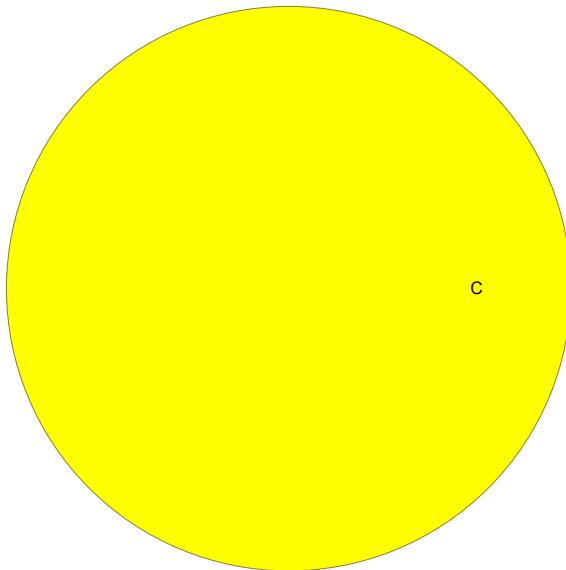
$$\begin{aligned}
& \frac{5}{6} \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2}, 1, \frac{13}{4}, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\frac{(a-b) \tan\left[\frac{1}{2}(e+f x)\right]^2}{a+b}\right] \\
& \sec\left[\frac{1}{2}(e+f x)\right]^2 \tan\left[\frac{1}{2}(e+f x)\right]\Bigg)\Bigg)\Bigg)\Bigg) \\
& \left(5(a+b) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\frac{(a-b) \tan\left[\frac{1}{2}(e+f x)\right]^2}{a+b}\right] + \right. \\
& 2 \left(-2(a-b) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \tan\left[\frac{1}{2}(e+f x)\right]^2, \right. \right. \\
& \left.\left.-\frac{(a-b) \tan\left[\frac{1}{2}(e+f x)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \right. \right. \\
& \left.\left.\tan\left[\frac{1}{2}(e+f x)\right]^2, -\frac{(a-b) \tan\left[\frac{1}{2}(e+f x)\right]^2}{a+b}\right]\right) \tan\left[\frac{1}{2}(e+f x)\right]^2\Bigg)^2 - \\
& \left(9 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\frac{(a-b) \tan\left[\frac{1}{2}(e+f x)\right]^2}{a+b}\right] \right. \\
& \tan\left[\frac{1}{2}(e+f x)\right]^2 \left(2 \left(-2(a-b) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \tan\left[\frac{1}{2}(e+f x)\right]^2, \right. \right. \right. \\
& \left.\left.\left.-\frac{(a-b) \tan\left[\frac{1}{2}(e+f x)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \right. \right. \right. \\
& \left.\left.\left.\tan\left[\frac{1}{2}(e+f x)\right]^2, -\frac{(a-b) \tan\left[\frac{1}{2}(e+f x)\right]^2}{a+b}\right]\right) \sec\left[\frac{1}{2}(e+f x)\right]^2 \tan\left[ \right. \right. \\
& \left.\left.\frac{1}{2}(e+f x)\right] + 9(a+b) \left(-\frac{1}{9(a+b)} 5(a-b) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \right. \right. \right. \\
& \left.\left.\left.\tan\left[\frac{1}{2}(e+f x)\right]^2, -\frac{(a-b) \tan\left[\frac{1}{2}(e+f x)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(e+f x)\right]^2 \right. \right. \\
& \left.\left.\tan\left[\frac{1}{2}(e+f x)\right]^2 + \frac{5}{18} \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \tan\left[\frac{1}{2}(e+f x)\right]^2, \right. \right. \right. \\
& \left.\left.\left.-\frac{(a-b) \tan\left[\frac{1}{2}(e+f x)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(e+f x)\right]^2 \tan\left[\frac{1}{2}(e+f x)\right]\right) + \right. \\
& 2 \tan\left[\frac{1}{2}(e+f x)\right]^2 \left(-2(a-b) \left(-\frac{1}{13(a+b)} 18(a-b) \operatorname{AppellF1}\left[\frac{13}{4}, \frac{1}{2}, 3, \right. \right. \right. \\
& \left.\left.\left.\frac{17}{4}, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\frac{(a-b) \tan\left[\frac{1}{2}(e+f x)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(e+f x)\right]^2 \right. \right. \right. \\
& \left.\left.\left.\tan\left[\frac{1}{2}(e+f x)\right]^2\right)\right)
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right] + \frac{9}{26} \text{AppellF1} \left[ \frac{13}{4}, \frac{3}{2}, 2, \frac{17}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, \right. \right. \\
& \left. \left. - \frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] \sec \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2 \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right] \right) + \\
& (\mathbf{a} + \mathbf{b}) \left( - \frac{1}{13 (\mathbf{a} + \mathbf{b})} 9 (\mathbf{a} - \mathbf{b}) \text{AppellF1} \left[ \frac{13}{4}, \frac{3}{2}, 2, \frac{17}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, \right. \right. \\
& \left. \left. - \frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] \sec \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2 \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right] + \right. \\
& \left. \left. \frac{27}{26} \text{AppellF1} \left[ \frac{13}{4}, \frac{5}{2}, 1, \frac{17}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, \right. \right. \\
& \left. \left. - \frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] \sec \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2 \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right] \right) \right) \right) / \\
& \left( 9 (\mathbf{a} + \mathbf{b}) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, - \frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] + \right. \\
& \left. 2 \left( -2 (\mathbf{a} - \mathbf{b}) \text{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, \right. \right. \right. \\
& \left. \left. \left. - \frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] + (\mathbf{a} + \mathbf{b}) \text{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \right. \right. \\
& \left. \left. \left. \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2, - \frac{(\mathbf{a} - \mathbf{b}) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2}{\mathbf{a} + \mathbf{b}} \right] \right) \tan \left[ \frac{1}{2} (\mathbf{e} + \mathbf{f} x) \right]^2 \right) \right)
\end{aligned}$$

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## Summary of Integration Test Results

4 integration problems



- A - 0 optimal antiderivatives
- B - 0 more than twice size of optimal antiderivatives
- C - 4 unnecessarily complex antiderivatives
- D - 0 unable to integrate problems
- E - 0 integration timeouts